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A brittle failure model for long-period seismic events recorded at Turrialba volcano, Costa Rica

Thomas S. Eyre ^{a, 1}, Christopher J. Bean ^a, Louis De Barros ^{a, 2}, Francesca Martini ^{a, 3}, Ivan Lokmer ^a, Mauricio M. Mora ^{b, e}, Javier F. Pacheco ^c and Gerardo J. Soto ^d

^a *Seismology and Computational Rock Physics Laboratory, School of Geological Sciences, University College Dublin, Belfield, Dublin 4, Ireland. tomyre2@gmail.com, Chris.Bean@ucd.ie, ivan.lokmer@ucd.ie*

^b *Escuela Centroamericana de Geología, Universidad de Costa Rica, San José, Costa Rica. mauricio.mora@ucr.ac.cr*

^c *Ovsicori-UNA, Universidad Nacional, Heredia, Costa Rica. jpacheco@una.ac.cr*

^d *Terra Cognita Consultores, San José, Costa Rica. katomirodriguez@yahoo.com*

^e *Red Sismológica Nacional (RSN: UCR-ICE), San José, Costa Rica*

¹ *Now at: Department of Physics, University of Alberta, Edmonton, AB, T6G 2G7, Canada. teyre@ualberta.ca*

² *Now at: Géoazur, Université de Nice Sophia-Antipolis, CNRS, Observatoire de la Côte d'Azur, 250 rue Albert Einstein, Sophia-Antipolis, 06560 Valbonne, France. debarros@geoazur.unice.fr*

³ *Now at: Tullow Oil Ltd, Dublin, Ireland. Francesca.Martini@tullowoil.com*

Corresponding Author: Thomas S. Eyre, Department of Physics, University of Alberta,
Edmonton, AB, T6G 2G7, Canada. (teyre@ualberta.ca)

Key Points

Pulse-like LPs have been inverted for their source locations and mechanisms

Scaling laws in the data are also investigated

Observations of LPs at Turrialba corroborate a brittle failure source model

Abstract

A temporary seismic network, consisting of 23 broadband and 6 short period stations, was installed in a dense network at Turrialba volcano, Costa Rica, between 8th March and 4th May 2011. During this time 513 long-period (LP) events were observed. Due to their pulse-like waveforms, the hypothesis that the events are generated by a slow failure mechanism, based on a recent new model by Bean et al. (2014), is tested. A significant number (107) of the LPs are jointly inverted for their source locations and mechanisms, using full-waveform moment tensor inversion. The locations are mostly shallow, with depths < 800 m below the active Southwest Crater. The results of the decompositions of the obtained moment tensor solutions show complex source mechanisms, comprised of high proportions of isotropic and low, but seemingly significant, proportions of compensated linear vector dipole (CLVD) and double couple components. It is demonstrated that this can be explained as mode I tensile fracturing with a strong shear component. The source mechanism is further investigated by exploring scaling laws

within the data. The LPs recorded follow relationships very similar to those of conventional earthquakes, exhibiting frequency-magnitude and corner frequency vs magnitude relationships that can be explained by brittle failure. All of these observations indicate that a slow failure source model can successfully describe the generation of short duration LP events at Turrialba volcano.

Index Terms: *volcanology; seismology; natural hazards*

Keywords: *volcano; seismicity; long period (LP) events; source inversion; Turrialba volcano; scaling laws*

1. Introduction

Turrialba volcano (3340 m.a.s.l.) is a stratovolcano located at the eastern edge of the Cordillera Volcánica Central, Costa Rica, Central America, 35km ENE of the capital San José (figure 1a). Activity at the volcano has increased in recent years, with intensifying fumarolic gas discharges, especially in the active Southwest Crater; summit inflation detected from 2005 to 2007; increases in seismicity; and recent minor phreatic explosions (Campion et al., 2012; Martini et al., 2010; Soto and Mora, 2013; Tassi et al., 2004; Vaselli et al., 2010). Monitoring the volcano is therefore extremely important, as its close proximity to San José means that a large eruption has the potential to adversely affect 1.5 million people (Soto et al., 2010).

A previous study was carried out into the source processes of long period (LP) seismic events recorded at Turrialba volcano in 2009 (Eyre et al., 2013), where LPs were inverted for their mechanism using full-waveform moment tensor inversion. Similar to studies conducted at other volcanoes, a crack source mechanism was obtained, in the case of Turrialba dipping shallowly towards the southwest. For the 2009 dataset this was interpreted, drawing on the Chouet (1986)

model of LP sources, as resonance within cracks in the hydrothermal system that follow weaknesses in the volcano edifice, or as hydrothermal fluids “pulsing” through the cracks. However, the authors state that a deformation-based source process could not be ruled out, as this was postulated as the cause of similar events observed on Mt Etna (De Barros et al., 2011).

A second experiment at Turrialba volcano was undertaken in 2011, building on the work carried out through the 2009 experiment and benefiting from the experience gained. The new experiment is one of the first to be designed specifically to obtain more accurate moment tensor inversion results for LP events, by incorporating more broadband seismometers into the network, especially in the summit region of the volcano. Enhanced coverage of the summit area has been demonstrated in previous studies to improve the moment tensor solutions (Bean et al., 2008; De Barros et al., 2011). As well as improved solutions, this is also a more in-depth study than that of Eyre et al. (2013), with moment tensor inversion applied to over 100 events.

During the experiment, Turrialba volcano was undergoing large-scale degassing, with up to ~ 3000 tonnes of SO₂ per day expelled into the atmosphere (Campion et al., 2012). The majority of this gas was released from a large fumarole located high on the southwest inner wall of the Southwest Crater, which opened during a minor phreatic eruption in January 2010. 20 broadband (five 60 s and three 30 s) and 6 short-period (1 s) seismometers were installed in a temporary network between 8th March and 4th May 2011, in addition to a 3 station permanent broadband network (stations VTCE, VTCG, VTUN). Figure 1b shows a map of the network. The non-active craters (the Northeast Crater and part of the Central Crater) allow for a dense deployment of stations in the summit region of the volcano. The network consisted of three seismic arrays and 13 stand-alone stations. Seismic arrays were located at TOMA, PIGA and BABO. TOMA consisted of the 6 short-period stations in the shape of a cross, with the long axis

pointing to the active Central and Southwest Craters and an inter-station spacing of approximately 60 m. The arrays BABO and PIGA consisted of 5 stations each, in a “T” shape with their long axes pointing to the summit region. All stations had a sampling rate of 100 Hz. The station WCR1 was located on the rim of the active Southwest Crater, within 100 m of the main fumarole, and WCR2 is also located on the crater rim. As the LPs in 2009 were located in this region at shallow depths (Eyre et al., 2013), it is likely both stations were very close to the source of the seismicity. However, the close proximity to the strong gas discharge caused these stations to record strong continuous energy in the 5 Hz to 40 Hz range.

There are currently two main categories of source models available for LP events: (1) the resonating crack/conduit model (Chouet, 1986; 1988; Neuberg et al., 2006), and (2) a very recently proposed slow brittle rupture model (Bean et al., 2014). In the first model, the lack of high frequency content of the events is explained by relating the source processes causing the events to fluid processes. A fluid-filled cavity is excited into resonance, inducing slow dispersive waves (crack waves) which propagate along the cavity interface, interfering constructively to produce the LPs observed. By definition this process leads to resonating seismograms. The second model attributes the low corner frequencies of the events to slow failure of unconsolidated volcanic material at shallow depths on volcanoes caused by the low internal friction angles of the material. Rupture simulations show that this process leads to pulse-like seismograms when not contaminated by path effects.

Examples of LP events recorded in 2011 and their corresponding spectra can be seen in figure 2, recorded on station WCR1, low pass filtered at 5 Hz to remove the strong noise due to degassing above this frequency. The main energy of the events is generally from 0.3 to 1.3 Hz. The events exhibit pulse-like waveforms and therefore the brittle failure model appears to be more likely to

fit the data, as there is no resonance in the waveform which would be expected according to the cavity resonance model. As the LP waveforms on Turrialba volcano are non-resonating, by analyzing the waveforms, source locations, source mechanisms and the scaling laws of these events, this study aims to determine if the slow failure model can reasonably explain the LP events observed on Turrialba volcano.

2. LP Event Identification

513 LP events were recorded between 8th March and 4th May 2011. These LPs are identified using the STA/LTA algorithm described in Eyre et al. (2013) for station TCCR, where the STA/LTA method is implemented for both a low frequency band (0.2 – 4.0 Hz) and a high frequency band (6.0 – 10.0 Hz) and the events are only picked when the STA/LTA value in the low frequency band is three times that of the high frequency band. An average of 9 events per day are detected.

LPs are filtered in a frequency band of 0.3 - 1.3 Hz (the frequency band in which they have most energy) and then correlated in an attempt to group them into families of similar events using a closed cluster technique (Eyre et al., 2013; Saccorotti et al., 2007) for 10 s windows of the Z component at summit station TCCR. No families of more than 5 events with a correlation coefficient greater than 0.75 could be found, suggesting that these events are not produced by a repetitive source. Hence the events are treated individually.

3. Full-Waveform Moment Tensor Inversion

3.1 Method

Following previous studies by Chouet et al. (2003), Kumagai et al. (2005), Kumagai et al. (2010), Nakano and Kumagai (2005), Ohminato et al. (1998) and Eyre et al. (2013),

simultaneous full-waveform moment tensor inversions to calculate the source mechanisms and grid searches for source locations are performed. The method is implemented identically to Eyre et al. (2013), with the exception of the velocity model. In the frequency domain, the n th component of the displacement u , recorded at position \mathbf{x} and frequency ω , can be written as:

$$u_n(\mathbf{x}, \omega) = G_{np,q}(\mathbf{x}, \omega) \cdot M_{pq}(\omega) + G_{np}(\mathbf{x}, \omega) \cdot F_p(\omega), \quad n, p, q \text{ in } \{x, y, z\} \quad (1)$$

where M_{pq} is the force couple in the direction pq , F_p is the single force acting in the direction p , and G_{np} and $G_{np,q}$ are the n th components of the Green's functions and their spatial derivatives with respect to the source coordinates, respectively, generated by the single force F_p and the moment M_{pq} , respectively. Green's functions are the displacement responses recorded at the receivers when an impulse force function is applied at the source position in an elastic Earth (the medium response). The summation convention applies. Equation (1) is linear, and in the frequency domain can be written in matrix form:

$$\mathbf{d} = \mathbf{G}\mathbf{m} \quad (2)$$

where \mathbf{d} is the data matrix, \mathbf{G} contains the Green's functions, and \mathbf{m} contains the moment tensor and single forces components. As the LP events are recorded in the near field, P- and S- waves are intertwined. The near field effect is accurately taken into account in our Green's functions calculations, allowing for a full waveform inversion. The quality of the inversion results is tested through the evaluation of the misfit between the calculated and the observed data, herein referred to as the residual R :

$$R = \frac{(\mathbf{d} - \mathbf{G}\mathbf{m})^T \mathbf{W} (\mathbf{d} - \mathbf{G}\mathbf{m})}{\mathbf{d}^T \mathbf{W} \mathbf{d}} \quad (3)$$

where \mathbf{W} is a diagonal matrix of weights for the quality of the data (in this study the data quality is good for all stations and components and therefore all of the weights are fixed to 1: the inversion intrinsically preferentially weights stations closer to the source). The inversion is carried out in the 0.3 - 1.3 Hz frequency band used for the correlations (section 2) for 12 s time windows, utilizing all components at all available stations.

In order to locate the events, the inversion is implemented for a grid of 2536 possible source points in a 4000 m by 4000 m by 2000 m volume below the summit region of the volcano (Chouet et al., 2003; Kumagai et al., 2005; Kumagai et al., 2010; Nakano et al., 2003; Ohminato et al., 1998), with a grid spacing of 80 m in the summit region and 200 m further from the summit. The number of possible source positions is much greater than the number of stations used in the inversion (15 stand-alone broadband stations are available for the inversion), so the Reciprocity Theorem (Aki and Richards, 2002) is used when computing the Green's functions between the sources and receivers. The most probable source location is defined by the grid point with the smallest misfit between observed and reconstructed data.

The Green's functions are calculated using a 3D elastic lattice method to simulate full-wavefield seismic wave propagation (O'Brien and Bean, 2004). The model includes topography which has been shown to be important for an accurate inversion in volcanic environments (Ripperger et al., 2003). The shallow velocity structure has also been shown to be important in inversions (Bean et al., 2008). As no model is currently available for Turrialba volcano (Eyre et al., 2013), the shallow velocity structure is investigated using surface wave dispersion analysis using the three available arrays (see section 1). The technique used is the multichannel analysis of surface waves (MASW) method (Wathelet et al., 2004). However, this analysis is very limited due to the small aperture of the arrays (the maximum station spacing is 180 m due to the steep

topography of the volcano). Although the results are confined to the very near-surface, analysis shows that a low velocity layer exists at Turrialba volcano as has been found on many other volcanoes (Bean et al., 2008, and references therein). Hence the numerical model used for simulating the Green's functions includes a low velocity layer of 1039 m/s (P-wave) and 600 m/s (S-wave), tracking the topography. However, as the surface wave inversion is not well constrained, and we do not want to include an unrealistic poorly constrained step in the model which would act as an unrealistic waveguide, we choose the smoothest model that fits the results. Therefore the velocities within the layer are gradated to 100 m depth, beneath which the model is homogeneous with a P-wave velocity of 2300 m/s and an S-wave velocity of 1328 m/s. Density is related via the equation $\rho = 1700 + 0.2v_p$, where v_p is the P-wave velocity (Gardner et al., 1974; O'Brien and Bean, 2009).

As the inversion is performed in the frequency domain without any assumption on the source time history, an inverse FFT of the solution **m** from the inversion of equation 2 leads to a source time function for every component of the moment tensor and single forces. In order to obtain a common source-time function, the moment tensor solutions are decomposed into their principle components, using the method of Vasco (1989). This method involves the singular value decomposition of the obtained six time-dependent moment tensor components. A common source-time function for all six moment tensor components and its contribution to each are obtained, thus giving a source-time history of the source process and its mechanism. The eigenvalues of the "static" moment tensor give the pressure and tension values along the principal axes (eigenvectors) from which the source mechanism can be reconstructed. From this, the solution can be decomposed into the percentage of isotropic, compensated linear vector dipole (CLVD) and double couple source mechanisms (Vavryčuk, 2001). Hence, for example, a

tensile crack source (often calculated as the most likely mechanism for LPs at volcanoes (e.g. Cusano et al., 2008; De Barros et al., 2011)) produces a $\lambda : \lambda : (\lambda + 2\mu)$ ratio of moment tensor eigenvalues (where λ and μ are the Lamé parameters) (Aki and Richards, 2002), which is 1 : 1 : 3 for a Poisson's ratio of 0.25 and 1 : 1 : 2 for a Poisson's ratio of 0.33.

Inversions are carried out both excluding and including single forces in the solutions. Single forces are physically realistic in volcanic environments (for example due to mass transfer, drag forces or volcanic jets) (Chouet, 2003; Takei and Kumazawa, 1994). However De Barros et al. (2011) and De Barros et al. (2013) state that errors in modeling the velocity structure mainly contaminate the single forces, leading to spurious single forces, while the moment tensor solution is still correct. In particular, De Barros et al. (2013) showed using radiation patterns that strong spurious forces, of the order of those usually derived from the moment tensors of real data, can be produced from the P-to-S conversions at the interfaces between two different materials. Since these interfaces are usually unknown in the shallow part of volcano, single forces cannot be taken into account when interpreting results. On the other hand, De Barros et al. (2011) suggest that the single forces will accommodate most of the errors, so they should be included in the inversion procedure but should not be interpreted as part of the source solution. Including single forces in the solution appears to stabilize the results obtained using the 2011 data and therefore this paper focusses chiefly on results for which single forces are included in the inversion procedure. The single forces themselves are not interpreted as even though they can be physically realistic in volcanic environments, they appear contaminated by model errors. Emphasis was also placed on the results which included single forces in the inversion procedure for the 2009 experiment (Eyre et al., 2013).

Constrained moment tensor inversion is also performed to test the robustness of the solutions, with the source mechanism constrained as (1) an isotropic source and (2) a crack with a grid search for the optimum dip and azimuth (for details, see Lokmer et al. (2007), De Barros et al. (2011)). We reiterate that the single forces terms can accommodate model errors (De Barros et al., 2013) and are therefore not physically interpreted. The number of data for every inversion is 3 components \times 15 stations \times N_f (number of frequency points). The number of unknowns decreases from $9 \times N_f$ for the moment tensor + single forces inversion to $6 \times N_f$ (moment tensor only inversion) and $4 \times N_f$ for crack + single forces constrained inversion.

As moment tensor inversion takes into account the amplitudes recorded at each station, site amplification effects between stations must be removed to gain accurate solutions. These are measured using the RMS amplitudes of the coda waves of several teleseismic earthquakes that were recorded during each experiment on all stations (e.g. Zecevic et al., 2013), filtered between 0.3 and 1.3 Hz. The earthquakes used were located between 1000 and 1500 km from Turrialba volcano and had magnitudes greater than 5.5 so that the coda for each event contained a measurable low frequency component.

As the LP events do not appear to group well into families, moment tensor inversion is carried out for a significant proportion (107 events, $\sim 20\%$) of all of the LP events observed. The events chosen are those with optimal signal-to-noise ratios (generally the larger events), in order to give an accurate inversion solution. We expect that inverting a large sample of LPs observed at Turrialba volcano will yield a representative picture of all LP seismicity at Turrialba volcano.

3.2 LP Location Results

Joint inversions and grid searches are implemented for 107 events, filtered between 0.3 and 1.3 Hz. An example of the results of the grid search location technique for a single event is shown in figure 3. The figure shows three slices through the grid of possible source locations used for the inversions, with each grid point colored according to the residual obtained in the moment tensor inversion for that grid point. The vertical slices are taken through the minimum residual, while the horizontal slice is located at a depth of 2660 m.a.s.l. (680 m below the summit). The most likely locations (the points with the lowest residuals) are shown in blue. It can be seen that the resolution in the horizontal plane is very good, with the location between the active Southwest and Central Craters, while the depth is less well constrained, but is less than 800 m below the summit.

Figure 4a shows the best locations for inversions including single forces for all 107 inverted events, in map view and W-E and S-N cross-sections. Most of the events are clustered tightly below the active Southwest and Central Craters above 2500 m.a.s.l., i.e. shallower than 800 m depth below the summit. The scattering in the source area may be due to uncertainty in the medium velocity, but as these events do not belong to a family it is not surprising that the sources are scattered in a region. The results in the x - y plane are consistent with the results of array analysis, and are also very similar to solutions obtained when single forces are not included in the inversion (figure 4b), demonstrating the robustness of the solutions. However the locations obtained when single forces are included in the inversion appear to cluster closer together and there are a smaller number of outliers than for inversions excluding single forces, suggesting greater reliability in the results.

3.3 LP Source Mechanism Results

261 Moment tensor inversion solutions for the source locations with the lowest residuals are
262 investigated by fixing the location and redoing the inversion. An example of the results from a
263 single LP event when single forces are included in the inversion is shown in figure 5. Note the
264 pulse-like waveforms of the obtained moment tensor solution. The normalized waveform fits
265 between the real and reconstructed data are also shown, showing good fits for the summit
266 stations but poorer fits at more distal stations due to the intrinsic weighting of the stations by
267 their recorded amplitudes. This is acceptable due to the strong oscillating path effects at stations
268 further from the source (Bean et al., 2014). An eigenvector diagram is also shown, constructed
269 using a method from Chouet et al. (2003) where the eigenvectors are calculated every 0.01 s
270 when the amplitude of one of the moment tensor components is greater than 90 % of the
271 maximum amplitude. Finally, as described in section 3.1, singular value decomposition (Vasco,
272 1989) is used to extract a common source-time function with the scalar moment tensor
273 containing its value for each component. The eigenvectors are oriented with the long
274 eigenvector 21° from vertical (this angle is herein named θ) and an azimuth anticlockwise from
275 east (herein named φ) of 332° , with eigenvalues of 1.0 : 1.2 : 1.8. From the moment tensor
276 decomposition of Vavryčuk (2001), this result is 74 % isotropic. However, there is one larger
277 eigenvalue and two shorter eigenvalues, suggesting that the mechanism can be described as a
278 crack. This is demonstrated in the decomposition where compensated linear vector dipole
279 (CLVD) components are found to contribute 18 % to the solution. If the source is a pure tensile
280 crack then the long eigenvector is orthogonal to the crack plane, hence θ gives the dip angle and
281 φ the dip direction. The results however also show a double couple component in both cases of 9
282 % . It is therefore difficult to visualize the source mechanism. We reiterate that the single forces

term tends to “absorb” model errors (De Barros et al., 2013) but the forces themselves are not reliable, and are not constrained further.

In order to determine whether these complex results are unique to this one LP event, 107 events are inverted and summarized in figure 6. The results of the moment tensor decomposition (Vavryčuk, 2001) (6a and b), and the orientations of the largest eigenvectors (θ and φ) (6c) are shown. Primarily the figure shows results for inversions where single forces are included, but figure 6a also shows results for moment tensor only solutions for comparison and completeness. The results of the principal component analysis are shown as histograms in figure 6a. The comparison between the results of inversions including and omitting single forces shows that similar distributions of results are resolved for each (i.e. similar peaks in the histograms), but the standard deviations in component percentages for inversions including single forces are much smaller. It is more likely that source mechanisms for LP events observed at the same volcano do not vary to a large degree, and therefore these findings corroborate the work of De Barros et al. (2013) who (as previously stated) suggest that moment tensor solutions from inversions including single forces are more reliable. This supports our decision to focus on results obtained when single forces are included in the inversions. Figure 6b shows the results including single forces as a triangular graph to show the full range of results. The triangular graph also shows the residual from the moment tensor inversion for each event using a color scale. A strong isotropic component is evident for all events, peaking at $\sim 75\%$. The CLVD and double couple components are much less significant but do appear to contribute, with the CLVD component peaking at $\sim 5\%$ but for some events contributing up to 40% , and the double couple peaking at $\sim 10\%$ but for some events up to 45% . The variability here, together with the different source-

time functions, is consistent with the LP events not presenting as families, i.e. events look different as the source mechanisms are different.

The mechanism orientations are shown in figure 6c, both for the unconstrained inversions (MT + F) and for inversions when the source is constrained as a crack mechanism with a grid search on the orientation (Crack + F). The color scale refers to the residuals obtained for the moment tensor inversion. The solutions obtained with the unconstrained inversions are compatible and validated with the crack constrained inversions, however the crack constrained inversions do not reproduce all the complexities associated with the unconstrained inversions. Although there is a large scatter in the results, it can be seen that for the majority of the events (especially when the residual is small) that θ is relatively small (30° or less). The cracks are therefore shallowly dipping, meaning that ϕ can be quite unstable. There also appears to be a preferential ϕ direction, with most events orientated with a ϕ of approximately 180° to 200° anticlockwise from east, i.e. due west, and perhaps a smaller cluster orientated roughly in the opposite direction (340° - 360° , due east). Therefore the cracks change dip around the horizontal position, from slightly eastward to the slightly westward dipping. Again, the variability in the orientations is consistent with the lack of similarity between event waveforms.

3.4 Joint Inversion and Grid Search Results: Discussion

The LPs are located at shallow depths below the volcano (< 800 m). The results for the events with the lowest residuals, suggesting the most reliable inversions, mostly give depths between 700 and 800 m below the summit, although this may be several hundred meters shallower or deeper due to the uncertainty in the velocity model which can strongly affect the depth determination. However, the shallow results are in good agreement with LPs previously

observed at Turrialba volcano (Eyre et al., 2013) and with results at other volcanoes, including Kilauea, Hawaii (Almendros et al., 2001), Campi Flegrei, Italy (Cusano et al., 2008), Mt Etna, Sicily (De Barros et al., 2009; De Barros et al., 2011; Lokmer et al., 2007; Saccorotti et al., 2007), Piton de la Fournaise, La Réunion (Zecevic et al., 2013), and Kusatsu-Shirane, Japan (Kumagai et al., 2002; Nakano et al., 2003).

Most of the events appear to be closely clustered together below the active Southwest Crater. This is again in good agreement with results from 2009 (Eyre et al., 2013). There are several events that appear to be outliers, however. It is most likely that these outliers are erroneous, as they generally have higher residuals and are poorly constrained. The shallow locations below the active crater suggest a relationship with shallow processes and this needs to be taken into account when interpreting the mechanisms.

The moment tensor inversion results suggest that the source mechanisms are strongly isotropic. However, the mechanisms also appear to have small CLVD and double couple components. As stated in section 3.1, the single force components are likely to be unreliable and are not interpreted physically. These results suggest a very complex source mechanism. An isotropic and CLVD mechanism combined is interpreted as a crack mechanism. With a small contribution from double couple included, the mechanisms could be interpreted as a crack mechanism with a small amount of shearing, akin to a transtensional or transpressional crack mechanism. A method for determining the mechanism parameters for this type of source is described in Vavryčuk (2001). A tensile earthquake (an earthquake with tensile faulting or combining shear faulting and tensile faulting) can be described using a slip vector that is not restricted to orient

within the fault plane and deviates from the fault plane, causing its opening or closing. This slip vector is labelled \vec{u} , and has an angle from the fault plane (labelled Σ) of α (figure 7a).

α and the λ/μ ratio (κ) at the source can be calculated using:

$$\kappa = \frac{4}{3} \left(\frac{c^{\text{ISO}}}{c^{\text{CLVD}}} - \frac{1}{2} \right) \quad (4)$$

$$\alpha = \sin^{-1} \left(3 \frac{M_{\text{max}}^* + M_{\text{min}}^*}{|M_{\text{max}}^*| + |M_{\text{min}}^*|} \right) \quad (5)$$

(Vavryčuk, 2001), where M_{max}^* and M_{min}^* are defined as the maximum and minimum deviatoric eigenvalues of the moment tensor solution, and c^{ISO} and c^{CLVD} correspond to the components of isotropic and CLVD energy, respectively. The angle between the normal to the fault and the tension (\vec{T}) axis is $\beta = 45^\circ - \alpha/2$, and this is also the angle between the slip vector and the tension axis. The angle (θ) between the tension axis and vertical is calculated using the eigenvectors of the moment tensor solution. From this, the orientation of the fault plane from vertical (δ) can be calculated using $\delta = \theta - \beta$.

The results are investigated for events with residuals obtained from the moment tensor inversion of less than 0.25 to remove events for which the mechanisms are more poorly resolved. Events with source locations that appear to be outliers are also removed. For the remaining 42 events the average of the double-couple components is 16 %, of the isotropic components is 72 % and of the CLVD components is 12 %. The standard deviations are 8 %, 8 % and 9 %, respectively. The relationship between α and the proportion of double-couple, isotropic and CLVD components can be plotted, as shown here in figure 7b (Vavryčuk, 2001) for the mean value of κ of 7.3. Low values of α correspond to a high degree of shearing as the slip vector is almost

parallel to the fault plane whereas high values of α correspond to tensile mechanisms. Using solutions with residuals lower than 0.25, the mean of the absolute values of α is 21° , while β is 34° , θ is 23° , and δ is -12° . The schematic geometry of the slip movement is shown in figure 7a, with the relationships between α and the percentage of isotropic, double couple and CLVD components (figure 7b). This shows that, even with a large value for the isotropic component, a small value of α can be found, i.e. the source mechanism does not deviate much from a shearing movement. Intuitively the results are very surprising as an α of 21° suggests a strong shear component and a low tensile component, apparently at odds with the small double couple component calculated from the decompositions of the solutions. Figure 7c shows a histogram of the distribution of α for all events inverted. There appears to be a large variability in α from -60° to 60° , and the standard deviation of α is 27° . Negative values of α suggest transpressional fracturing and positive values suggest transtensional fracturing, however due to potential errors from mismodeling the velocity structure we do not believe that it is possible to accurately resolve the polarity of α . The low angles calculated for α therefore strongly support the possibility of a combined tensile-shear mechanism. Double couple components have been observed in other studies of LP events (Cusano et al., 2008). However, as the principal models of LP source mechanisms attribute them to fluid oscillation processes, these components are often interpreted as insignificant, or explained as errors resulting from the calculation of the Green's functions. In such cases, it is possible to interpret the source mechanism as a crack, as was construed in the 2009 study of Eyre et al. (2013). However as the double couple component is similar in size to the CLVD component it would be difficult to justify including the CLVD component in the interpretation while ignoring the double couple.

If the LP source is truly a tensile-shear mechanism, unidirectional slip motion should be observed in the source-time function, i.e. the band-limited response to a ramp function. To investigate whether this is the case, the source-time function obtained from singular value decomposition of the moment tensor solution for an LP event is shown plotted in figure 8a, along with the band-limited signal (band-pass filtered between 0.5 and 1.3 Hz) produced by the ramp function shown in figure 8b which has a rise time of 0.5 s. As expected, the onset and overall shape of both signals are similar; however the LP source-time function shows some extra higher frequency fluctuations later in the signal. These could be caused by errors in the inversions such as mismodeling of the velocity structure, leading to some path effects mapping into the source-time function. Nevertheless as the mechanism has a tensile component the source-time function is likely to be more complicated than in the case of simple shear. The opening of a crack is followed by a closing, as the pressure within strongly decreases during opening (Eaton et al. 2014). This means that tensile mechanisms only exhibit a small unidirectional movement. In the case of LP events at Turrialba volcano, as the source is complex, involving both the opening and closing plus shearing of the crack, the source-time function is also more complex than for the simple shearing case, which may explain the source-time function observed. The source-time function that we reconstruct is therefore fully compatible with a tensile-shear mechanism.

The obtained κ values should provide an indication of the fractured material. The mean κ value of 7.3 corresponds to a Poisson's ratio of ~ 0.44 . Such high values suggest that the source region either consists of (1) highly fractured or porous media saturated with fluids (as P-wave velocities are driven by the fluids, while S-wave velocities depend on the solid frame), or (2) ductile media (which may or may not be caused by high temperatures). For example, dense sands (which have a ductile response to stress and are likely highly similar to the unconsolidated material typically

found at the near-surface in the summit regions of volcanoes) have a Poisson's ratio of 0.45 (Greaves et al., 2011). As fluids, structural heterogeneities, unconsolidated materials and high temperatures are likely to be present in the shallow part of the volcano, either of these are strong possibilities. However, it must also be taken into account that the obtained value of κ can be strongly influenced by the accuracy of the velocity model.

4. Scaling Laws of LP Events

The results outlined above show that the events are caused by a tensile mechanism with a likely strong shear component. These results can be well explained by the new source model for LP events of Bean et al. (2014) where the events are generated by slow failure in the shallow edifice. However, further analysis of the LP events is necessary to investigate how well the model corroborates the data and to explore brittle failure as a valid model. Tectonic earthquake seismology uses empirical scaling laws to link the seismological observations to the source properties, and the above observations encourage us to apply such analysis to these LP data to further investigate their source.

4.1 Frequency-magnitude relation

The frequency-magnitude relation (Gutenberg and Richter, 1944; Ishimoto and Iida, 1939) usually gives a b -value of approximately $b = 1$ for tectonic earthquakes. Figure 9 shows a plot of the LP event maximum amplitudes (plotted logarithmically to use as a proxy for magnitude) against the cumulative number of events for the LPs observed at Turrialba volcano during the 2011 experiment, recorded on station TCCR (which has a higher signal-to-noise ratio than WCR1). Amplitude can be used as a proxy for magnitude only for earthquakes which are at the same distance from the station, which is satisfied here. It is noted that the slope of cumulative

number versus amplitude in log-log plot is actually known as the m -value (Ishimoto and Iida, 1939). Above the visually estimated detection threshold of $\sim 3 \times 10^{-6}$ m/s the relationship appears to show non power-law scaling with a deficit of larger events.

One possible interpretation for this behavior is that the steepest gradient (-2.9, line shown in figure 9) corresponds to the true b -value and the real detection threshold is $\sim 2 \times 10^{-5}$ m/s. Note that here we assume that amplitude is proportional to the magnitude ($b = m$), but even if we assume a relationship of $m = b + 1$ instead (Suzuki, 1959), we obtain $b = 1.9$ which is still higher than that observed for ordinary earthquakes. The smaller events (amplitude $< 2 \times 10^{-5}$ m/s) do not fit the relationship due to the variable levels of noise (e.g. volcanic tremor) resulting in an incomplete catalogue. Other potential issues include the relatively small size of the catalogue and the small magnitude range of the catalogue (~ 2 orders of magnitude). For amplitudes below $\sim 3 \times 10^{-6}$ m/s, the graph is flat as the events are no longer detectable. In this interpretation larger LPs occur less often than expected based on the typical earthquake scaling law. However, large b -values have been observed for earthquakes and volcano-tectonic (VT) events in volcanic areas, e.g. at Mt. St. Helens and Mt. Spurr (Wiemer and McNutt, 1997), Mt. Pinatubo (Sánchez et al., 2004) and the off-Ito volcanic region (Wyss et al., 1997), so this is also feasible for LPs. Warren and Latham (1970) state that b -values up to 3 are possible in earthquakes induced by high thermal gradients, supported by Wiemer and McNutt (1997). Another possibility is that the high b -value could be caused by high heterogeneity of the material where the fracturing occurs (Mogi, 1962) and/or a low stress regime (Schorlemmer et al., 2005), both of which are highly likely at shallow depths on volcanoes. Finally, Wiemer and McNutt (1997) also propose that increased pore pressure due to heating of the groundwater could increase pore pressure and so lower effective stress, which is also very likely at shallow depths beneath the Southwest Crater at

Turrialba volcano. The high b -value of the LPs could therefore be caused by a combination of these factors.

Nonetheless, it is felt that the section of the graph with a lower gradient occurs over a much larger range of amplitudes than would be expected if it was caused by incompleteness of the catalogue. Therefore the behavior is interpreted as a real manifestation caused by the source processes of the events. Bean et al. (2014) observed a similar non power-law scaling for failure at the brittle-to-ductile transition in materials similar to those observed at the near-surface of volcanoes simulated using a damage mechanics model. They also stated that this relationship is very similar to magnitude-frequency relationships of LPs observed at Mt. Etna, Sicily and at Turrialba volcano during the 2009 experiment. The observations made here are consistent with these earlier findings.

4.2 Corner frequency analysis

Earthquakes follow a corner frequency (f_c) versus magnitude (M_0) scaling. The most commonly used relationship is $M_0 \propto f_c^{-3}$ (Aki, 1967; Geller, 1976; Hiramatsu et al., 2002; Kanamori and Rivera, 2004). Before this analysis is performed, we must first confirm that the LP spectra appear similar to earthquake spectra, with flat spectra up to a corner frequency where the energy begins to fall off (the fall off is often modeled using an ω^{-2} model). The unfiltered displacement spectrum for the event from figure 2a is plotted in log-log scale in figure 10. This shows that the events do behave like typical earthquakes, and a corner frequency can be picked. As previously mentioned, the peak above 10 Hz corresponds to continuous noise (spectral estimates for pre-LP signal noise are plotted in blue).

4.2.1 Synthetic Tests

A concern with implementing corner frequency analysis on LP events at volcanoes is that the LPs are recorded in the near field and have a tensile component, since the corner frequency concept is valid in the far field approximation for double couple mechanisms. On a theoretical basis, Eaton et al. (2014) show that the corner frequency relationship is still valid for events with tensile components. To investigate whether the corner frequencies can be accurately recovered in the near field, synthetic tests are conducted.

The Stokes solution of elastic wave radiation (Aki and Richards, 2002; Lokmer and Bean, 2010) is used to kinematically calculate synthetic seismograms. The near field and intermediate field effects can be included in the calculations. In order to simulate finite fault ruptures, the source comprises a 2D grid of “tensile crack” point sources representing the rupture plane. These point sources rupture unilaterally along the longer dimension of the rupture plane. In order to yield a range of event magnitudes the rupture plane ranges in size from 50 m to 1000 m long (with the width equal to half of the length).

To test whether the relationship should hold specifically for the LP events recorded at Turrialba volcano with the stations used, the rupture plane is located in a similar location to the recorded LP events (UTM 196920 m E, 1108760 m N and 2660 m.a.s.l.), and has a similar orientation with $\theta = 20^\circ$ and $\varphi = 190^\circ$. The first station tested is WCR1, which has the highest amplitudes and least propagation effects for the events as it is closest to the source, and therefore would be the optimum station to employ for source property studies.

In order to find the corner frequencies, the spectra of the synthetic events are fitted to the ω^{-2} model using the equation:

$$A = \frac{1}{\sqrt{1 + \left(\frac{f}{f_c}\right)^4}} \quad (6)$$

where f is the frequency and f_c is the corner frequency (e.g. Abercrombie, 1995). The fit is implemented for a range of corner frequencies to find the corner frequency with the optimum least-squares fit between the equation and the data. The fit also outputs the amplitude for the flat part of the spectrum of the event, which is used as a proxy for the magnitude.

The relationship between corner frequencies and magnitudes for the synthetic events in the far field is shown in figure 11a, along with the fits between the spectra and fitting function. A strong inverse relationship between the two is demonstrated as expected. The relationship is not quite f_c^{-3} as is expected (the slope of the best fit line is -3.45 instead of -3). When the near field (and intermediate field) term is included, invalidating the far-field assumption, the results are worse, but an inverse relationship can still be recognized with a slope of -5.03 (figure 11b). To check that this is a real problem caused by the close proximity to the source, the analysis is also carried out at a station further from the source, station DIVI. Here the analysis results in gradients of -3.13 and -2.57 excluding and including the near field term, respectively, much closer to the expected solution of -3.

4.2.2 Analysis of LP Data

The synthetic analysis has shown that ideally a far field station should be used for the analysis in order to reduce the near field effect. Unfortunately this is not possible as these stations have much larger propagation effects included in the LP spectra (Bean et al., 2008) which can strongly affect the results of seismic source studies (Giampiccolo et al., 2007), have a lower signal-to-noise ratio and have a smaller range of LP event amplitudes. Therefore station WCR1, on the

rim of the active Southwest Crater, is used for the analysis. The synthetic tests have demonstrated that the gradient of the best fit of the data cannot be interpreted but if an inverse relationship is uncovered this still has implications for the source mechanism.

As the LPs recorded are relatively small (of the order of 1×10^{-5} m) in comparison to the earthquakes usually analyzed using this method and the noise is quite high (as shown in figure 10), it is very difficult to determine the corner frequencies of the events. In order to overcome this issue, the following procedure is implemented. The events are first extracted and cut into 10 s long traces before integrating into displacement. Their means and trends are removed, the traces are tapered using a Hann window and are then transformed into the frequency domain. The spectra are smoothed using a moving average. Corner frequencies of the events can now be obtained using the same technique used for the synthetic data. Fits are implemented for a frequency range of 0.3 to 7.0 Hz, just above the microseismic noise range.

The results of the analysis are shown in figure 12a. Figure 12b shows examples of the fit of the ω^{-2} model used to calculate the corner frequencies with the data spectra of random individual events. It can be seen that there does appear to be a relationship between the corner frequency and the magnitude of the events. The L1 norm best fit has a gradient of -2.0 rather than the -3.0 expected in the dry, brittle fracture of earthquakes when analyzed in the far field. However, as the noise and the distribution of the event sizes can bias the linear regression, we computed two L1 norm linear regressions: the corner frequency as a function of the amplitude and the inverse relationship. The average value we obtain for the gradient is -2.9, which is very close to the -3.0 expected. Therefore the f_c^{-3} relationship is consistent with the data. The observed inverse relationship is consistent with a brittle failure origin for the Turrialba volcano LP events.

5. Discussion

The observations and results presented in this paper corroborate the possibility that LP events at Turrialba volcano may be generated by a failure mechanism. First, LPs observed close to the source (i.e. at the summit stations) are often pulse-like, and this is evidence that especially conflicts with the Chouet (1986) model of fluid-filled cavity resonance. This fact could be explained by a high damping of the resonance due to a high viscosity fluid or low crack wall stiffness (Chouet, 1986), but it seems suspicious that a model to describe resonance should apply for pulse-like waveforms. On the other hand, a material failure model does not require such specific tuning.

Second, the frequency-magnitude relationship and corner frequency-magnitude relationships are very similar to those observed in rock fracture experiments and earthquake studies. More work is required to analyze whether other possible source mechanisms or triggers can cause the relationships observed, but this goes beyond the scope of this paper. Together though, these observations appear to suggest that a mechanical failure mechanism is more likely than a resonant mechanism for LP event generation at Turrialba volcano.

Finally, the results from the moment tensor inversion suggest a tensile mechanism with a strong shear component. This is difficult to explain using the Chouet (1986) model but can readily be explained using the model of Bean et al. (2014) as tensile (mode I) cracks combined with shearing, which results in transtensional- or transpressional-like faulting. Transtensional faults seem especially plausible in volcanic environments due to flank instabilities and hydrofracture in hydrothermal systems, and transpressional faults could be caused by gravitational collapse. Dipping slump faults have been mapped at volcanoes, for example Stromboli (Apuani et al.,

2005), and shallow-dipping detachment faults have been proposed at Mt. Etna (Rust et al., 2005). In the case of Stromboli, a VLP event was constrained as a slow-slip double couple event caused by dip-slip (Cesca et al., 2007). This type of faulting fits well with the orientations of the mechanisms obtained for the LPs at Turrialba volcano, as they have shallow dip angles. Turrialba volcano sits within a SW-NE trending graben structure with a strike-slip component of motion (Soto, 1988), however linking the tectonic regime to the LP mechanisms is very difficult in the shallow part of the volcano as the stress regime can be completely altered by the presence of fluids, topography effects, gravitational instability and structural heterogeneities near the summit.

A likely underlying cause of the events observed at Turrialba volcano therefore appears to be deformation. The majority of the events are located below the active Southwest and Central Craters, as was also constrained for events recorded in 2009 (Eyre et al., 2013). This suggests that small-scale deformation is occurring below these active craters. However, the recovered source-time function is not accurate enough to distinguish between inflation, which could be caused by an influx/rising of magma or hydrothermal processes, and deflation, which could be due to the loss of large quantities of gas and edifice collapse. As previously mentioned, large scale deformation has not been observed at Turrialba volcano since 2007 (Martini et al., 2010) so the deformation causing LP events is likely to be small and localized beneath the active craters.

Future work is necessary to explore the slow failure model for LP event generation as described by Bean et al. (2014), however the observations and analysis described in this paper suggest that brittle failure is a possible LP generating mechanism on Turrialba volcano.

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Figure Captions

Figure 1 – (a) Map of the location of Turrialba volcano in Costa Rica. (b) Map of the 2011 broadband seismic network at Turrialba volcano, including an inset enlarged map of the summit region. Solid triangles indicate stand-alone seismic stations and open triangles denote arrays of

stations. The approximate positions of the summit craters are outlined by red dashed lines,
labelled SW, C and NE to denote the Southwest, Central and Northeast Craters, respectively.
Contours are in m.a.s.l..

Figure 2 – (a) - (d) Examples of LP events recorded on the vertical component of summit station
WCR1 (shown filtered between 0.3 and 1.3 Hz in red as used in the moment tensor inversion)
and the corresponding frequency spectra. The events are low-pass filtered below 5 Hz to remove
the strong noise above this frequency believed to be caused by the strong degassing.

Figure 3 – Location of the LP event shown in figure 2a calculated using full waveform moment
tensor inversion for a 3D grid of possible source locations below the volcano. Low residuals
(blue) indicate likely locations. The vertical slices are through the point with the minimum
residual. The horizontal slice is located at 2660 m.a.s.l.. The result when single forces are not
included in the inversion is very similar. The optimum location is at shallow (< 800 m) depth
below the active Southwest (or edge of the Central) Crater.

Figure 4 – Location results for all 107 inverted LP events obtained using the moment tensor
inversion grid search method. Results for inversions including (a) and excluding (b) single
forces are shown. The colored markers show the location of the minimum residual for each
event, with the color and marker size corresponding to the number of events. The locations are
shown in map view (top panel) and west – east and north – south cross-sections (bottom left and

right respectively). The map view shows contours in m.a.s.l.. In both cases most of the events are located below the active craters at shallow depths, however the results from inversions including single forces are more tightly clustered, with fewer outliers.

Figure 5 – Results of the full waveform moment tensor inversion for the event shown in figure 2a for the source location with the lowest residual. The moment tensor solution (including single forces) is shown top left, and the normalized waveform fits between the real (blue) and reconstructed (red) data below (traces are 12 s long). The eigenvectors, sampled every 0.01 s, of the moment tensor solution are also plotted (right).

Figure 6 – Collective results from the full waveform moment tensor inversion of all 107 LP events. (a) The results of the principal component analysis from Vavryčuk (2001), with the moment tensors decomposed into their proportions of isotropic, CLVD and double couple components, for inversions excluding (MT) and including (MT + SF) single forces in the solutions. The results are similar in both cases, but solutions including single forces show much less spread, suggesting that they are less affected by errors in the inversion procedure. The results are also illustrated for inversions including single forces in (b) in a triangle graph, to more easily visualize the relationships for individual events. The residuals obtained for each inversion are also shown according to the color scale. The results show a strong isotropic component for most events, with lower but significant components of CLVD and double couple. (c) The orientations of the principle eigenvectors for the unconstrained and crack constrained inversions including single forces. Again the color scale indicates the residual obtained from the inversion.

θ is small for most events. For the events with low residuals, φ appears to be preferentially orientated to $180^\circ - 200^\circ$ anticlockwise from east.

Figure 7 – (a) Average source mechanism for LP events with moment tensor solutions with residuals lower than 0.25, plotted using the method of Vavryčuk (2001). The slip vector is labelled $[\vec{u}]$, the fault plane is labelled Σ and \vec{T} is the tension axis. α is 21° , θ is 23° , and δ is -12° . (b) Relationship between α and the double-couple (DC), isotropic (ISO) and CLVD components for the source mechanisms of events with $\kappa = 7.3$ (corresponding to a Poisson's ratio of ~ 0.44) at the source, using the relationship of Vavryčuk (2001). (c) Histogram of the number of events with slip vector orientated for each 10° range of α .

Figure 8 – (a) Comparison between the source-time function obtained from singular value decomposition of the moment tensor solution of an LP event from Turrialba volcano, filtered between $0.5 - 1.3$ Hz (blue) and the signal obtained by filtering the ramp function with a rise time of 0.5 s (b) in the same frequency band (red). Note the similarities between the two signals: the first peak and overall shape. Higher frequency fluctuations observed later in the decomposed signal may be caused by errors in the inversion procedure or may be due to the complex interaction within the source of unidirectional shearing plus tensile opening and closing.

Figure 9 – LP event amplitudes (plotted in logarithmic scale as a proxy for magnitude) against cumulative number of events greater than that amplitude. The catalogue appears to be complete

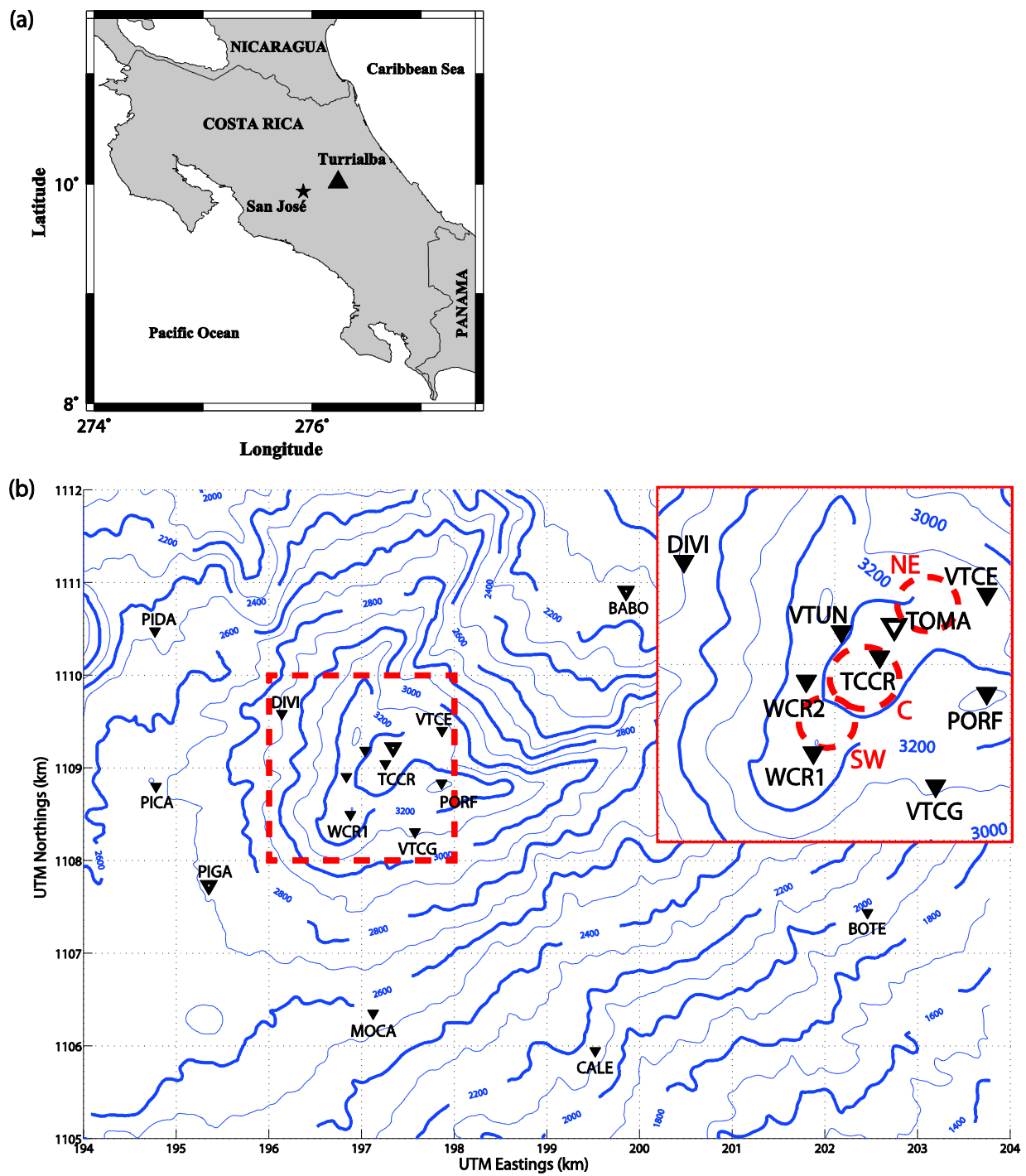
above the visually estimated detection threshold of $\sim 3 \times 10^{-6}$ m/s. The line of best fit for the steepest section of the plot has a gradient of ~ -2.9 .

Figure 10 – Displacement frequency spectrum of the LP event from figure 2a recorded at WCR1, in log-log scale (black). The noise spectrum taken before the event is also shown (blue), demonstrating that the event spectrum is above the noise. The shape of the spectrum appears similar to that of a regular earthquake, allowing a corner frequency to be picked. The peak above 8 Hz corresponds to continuous noise and so is ignored in the corner frequency analysis.

Figure 11 – Relationship between corner frequency and magnitude for synthetically created events located in a similar location to the real events and recorded at station WCR1. Also shown are the fits between the synthetic event spectra and the function used to estimate the corner frequencies. L denotes the length of the rupture plane. (a) shows the results for the far-field term only, and (b) shows the results including the near-field term. The best fit lines are shown: (a) has a slope of -3.45 and (b) has a slope of -5.03 . For ordinary earthquakes, -3 is expected. The results suggest that the corner frequencies of events are affected by recording close to the source, especially by the near-field term, however an inverse linear relationship is always present.

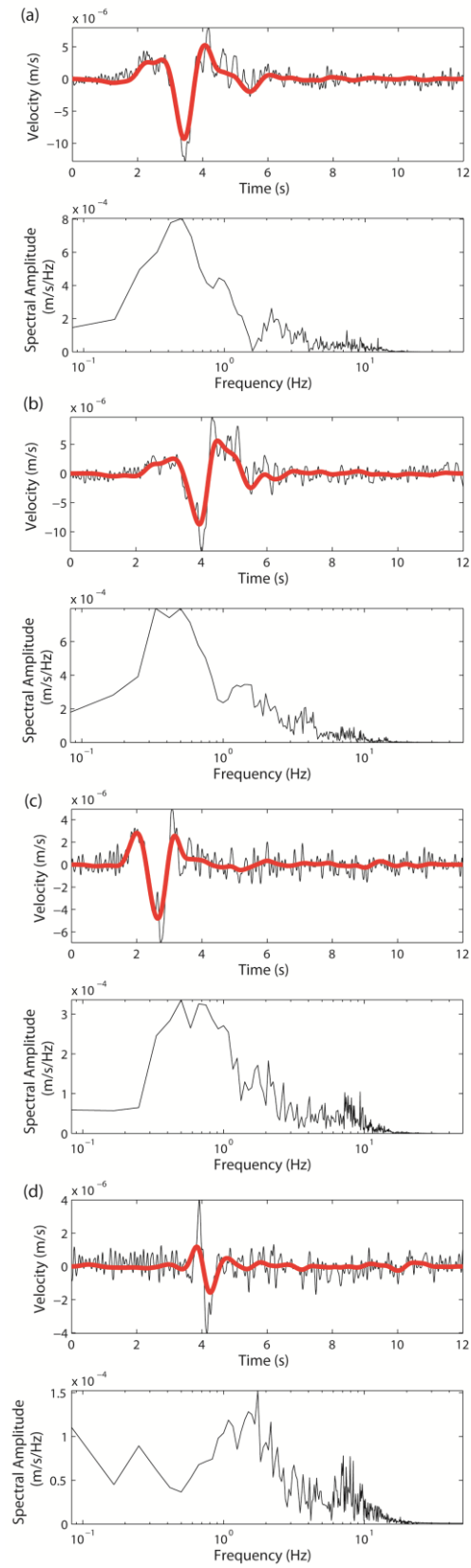
Figure 12 – Relationship between corner frequency and magnitude for LP events recorded at Turrialba volcano for station WCR1. (a) shows the results from the corner frequency analysis of the LP events. As the magnitude range is small and the fits are not exact, the events are quite

clustered, but there does appear to be a clear inverse relationship between corner frequency and magnitude. A line of best fit (calculated using the L1 norm) is plotted through the data (red line), with a slope of -2.04. A second line of best fit has also been calculated using the inverse of the relationship, as the noise and the distribution of the event sizes can bias the linear regression and is plotted as a dashed red line, with a gradient of -3.76. The theoretical -3 earthquake relationship is also plotted (black with markers) and is also consistent with the data. (b) shows examples of the fits between the smoothed spectra of 9 random LP events (blue), and the fitting functions (red). The fits appear to be reasonable.



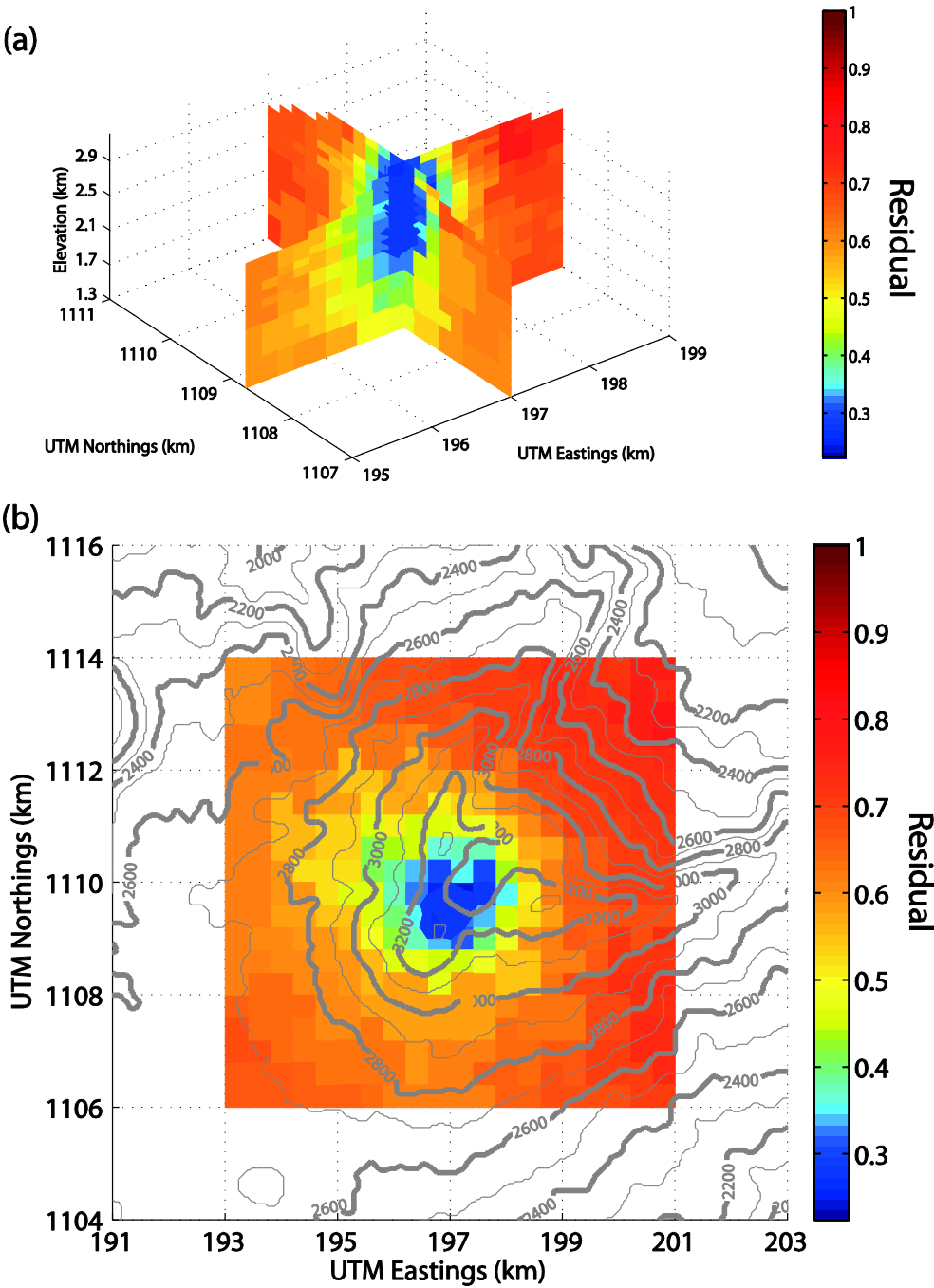
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889 Figure 1



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891 Figure 2



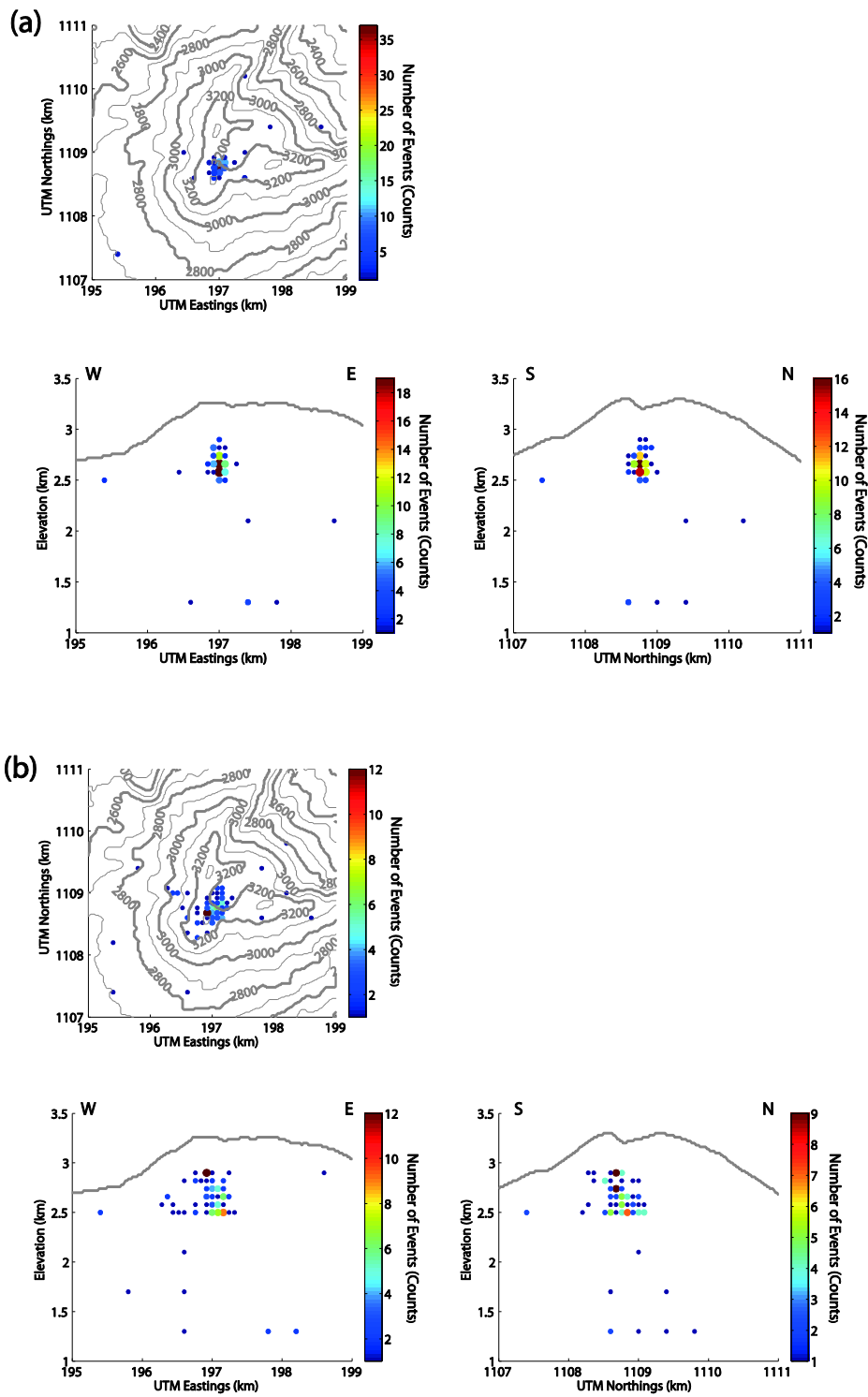
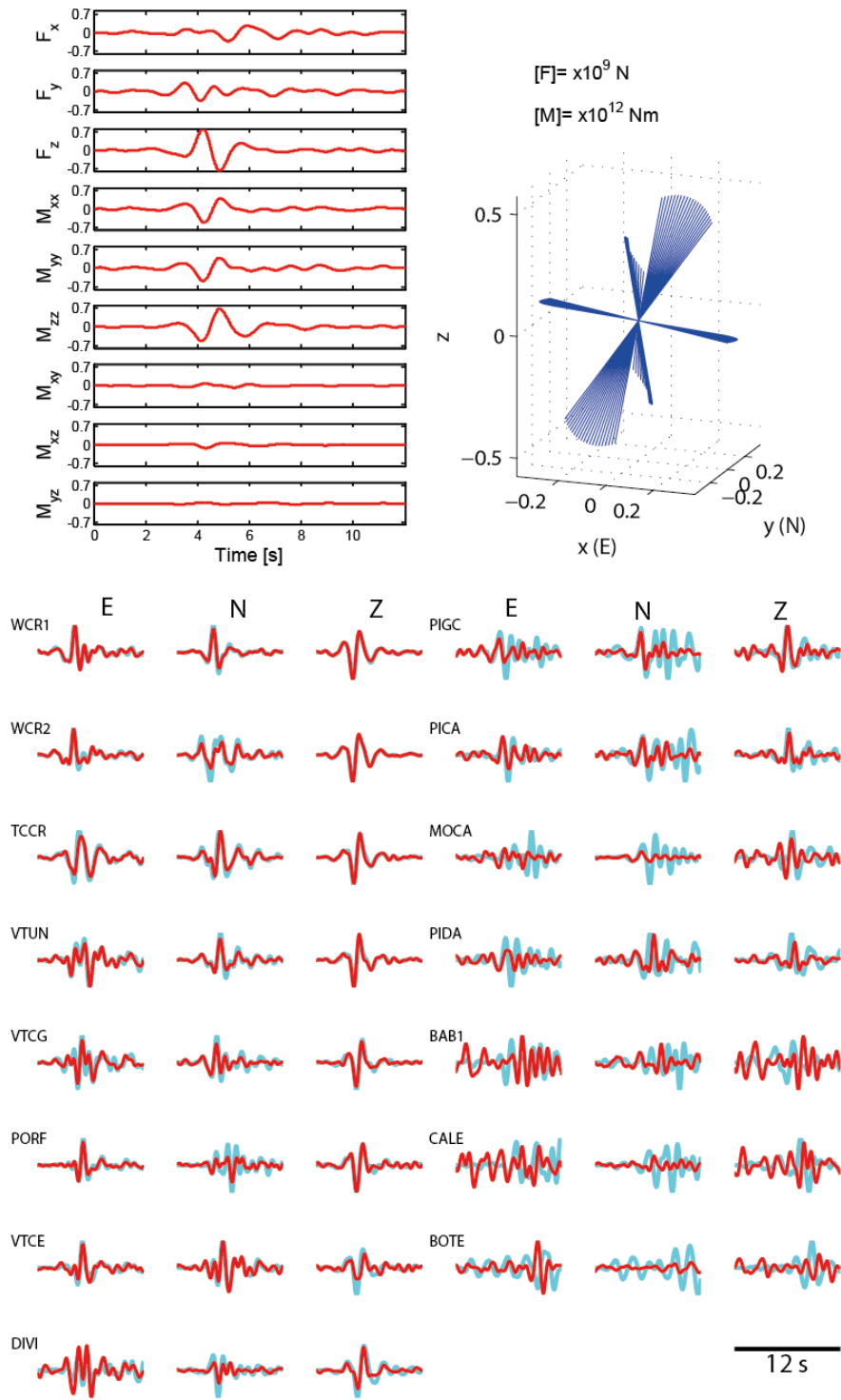


Figure 4



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900 Figure 5

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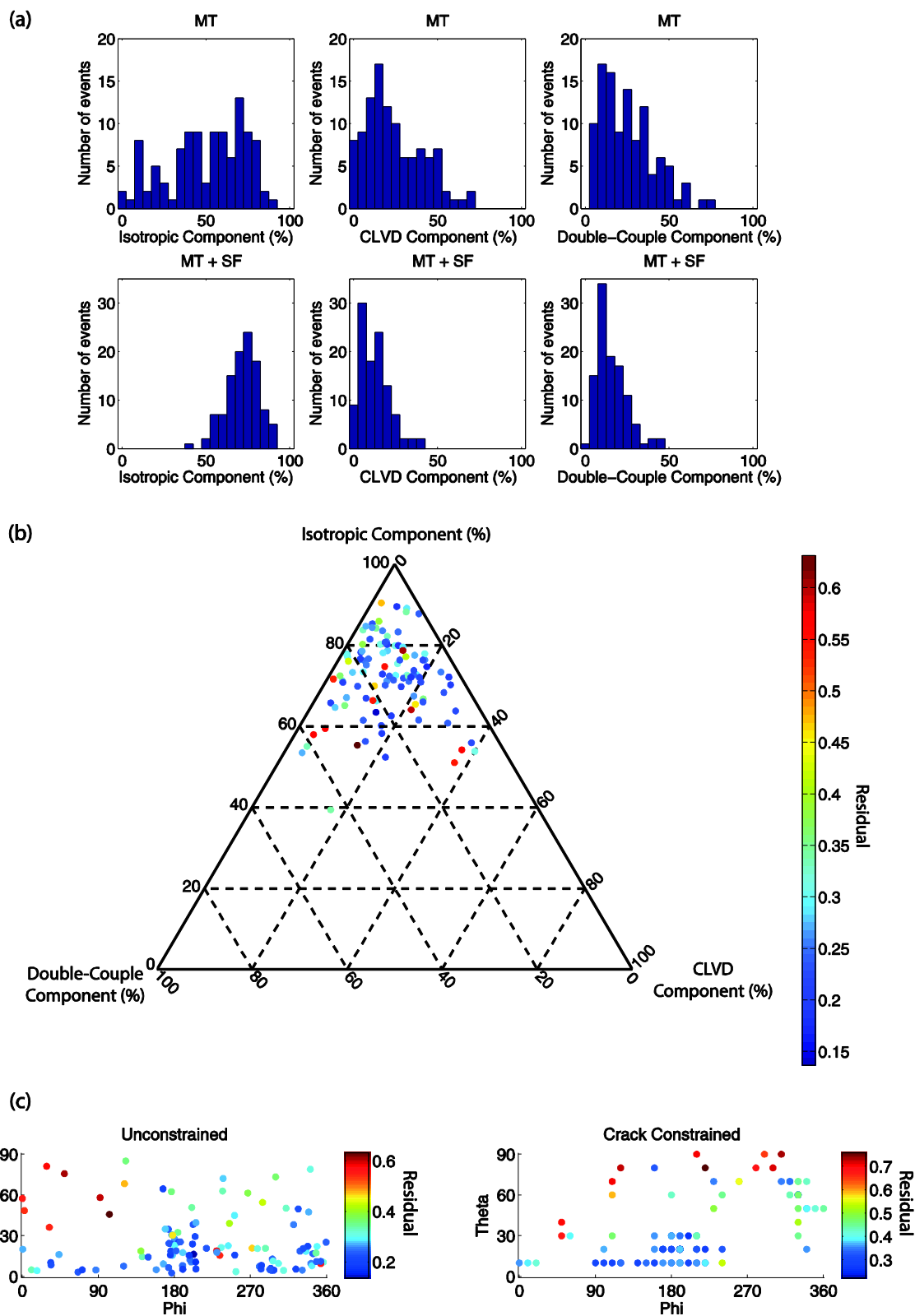
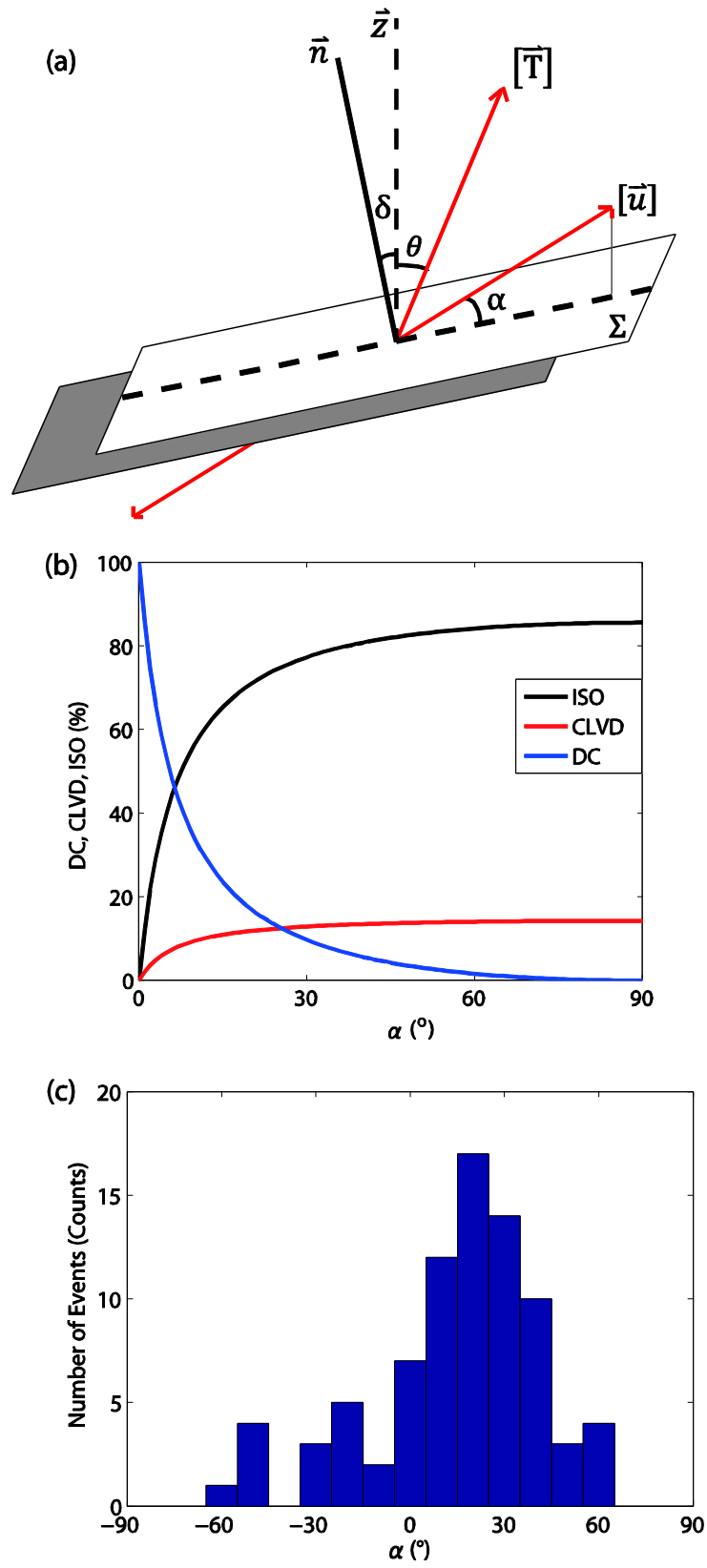
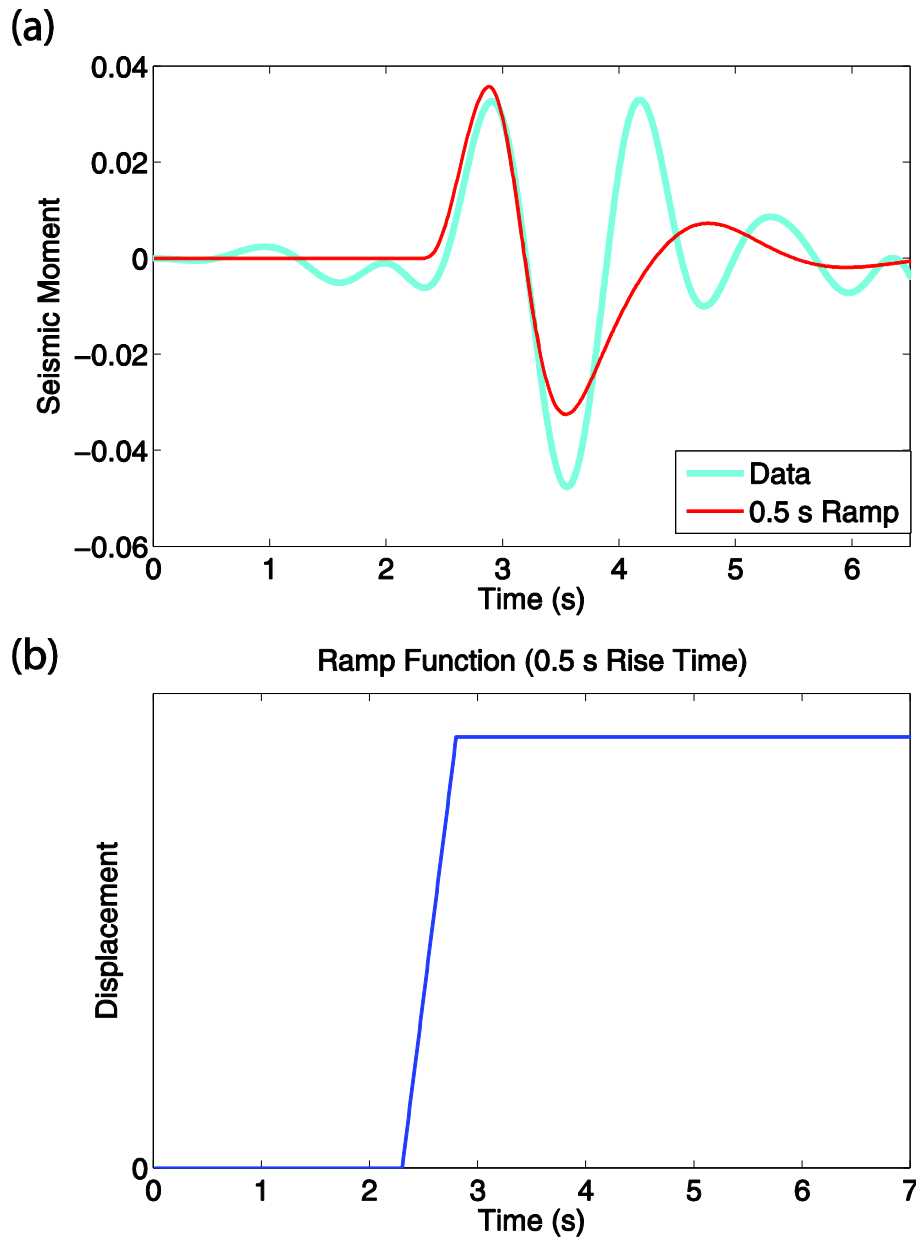


Figure 6



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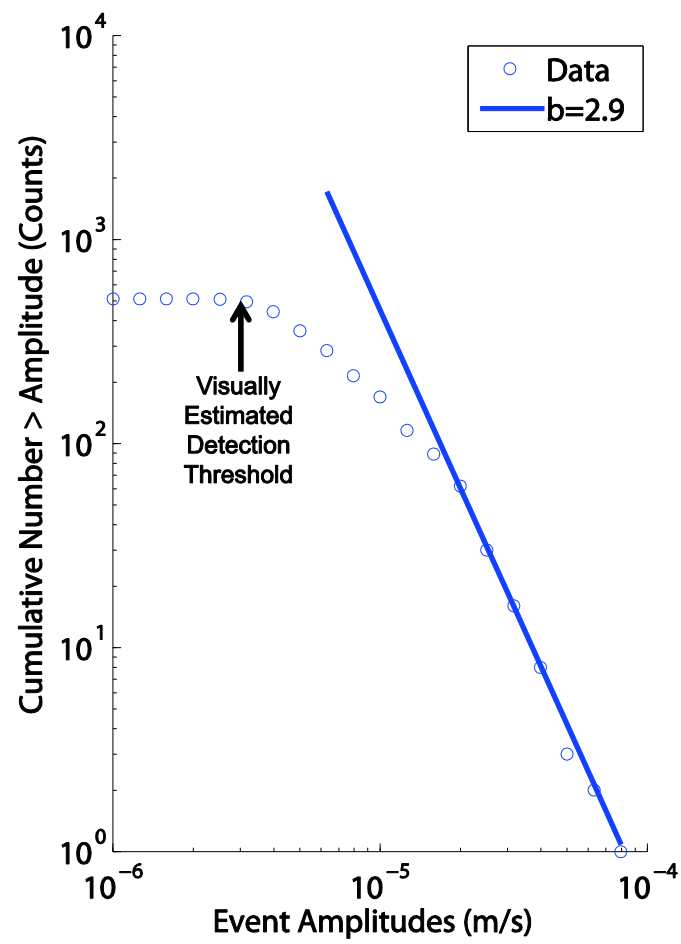
905 Figure 7



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908 Figure 8

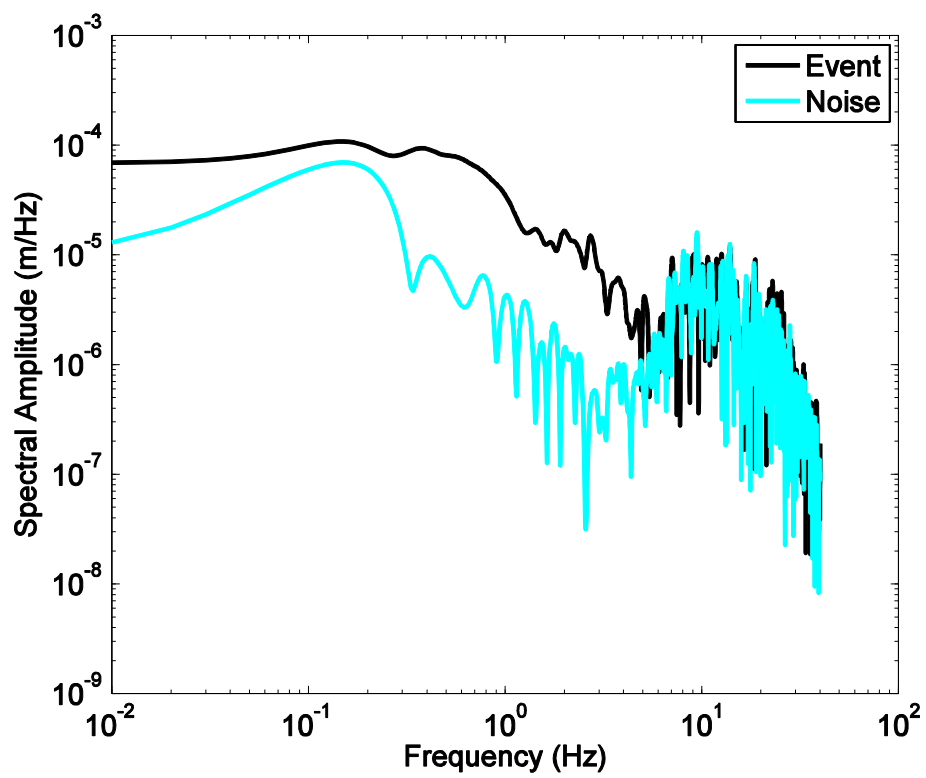


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910 Figure 9

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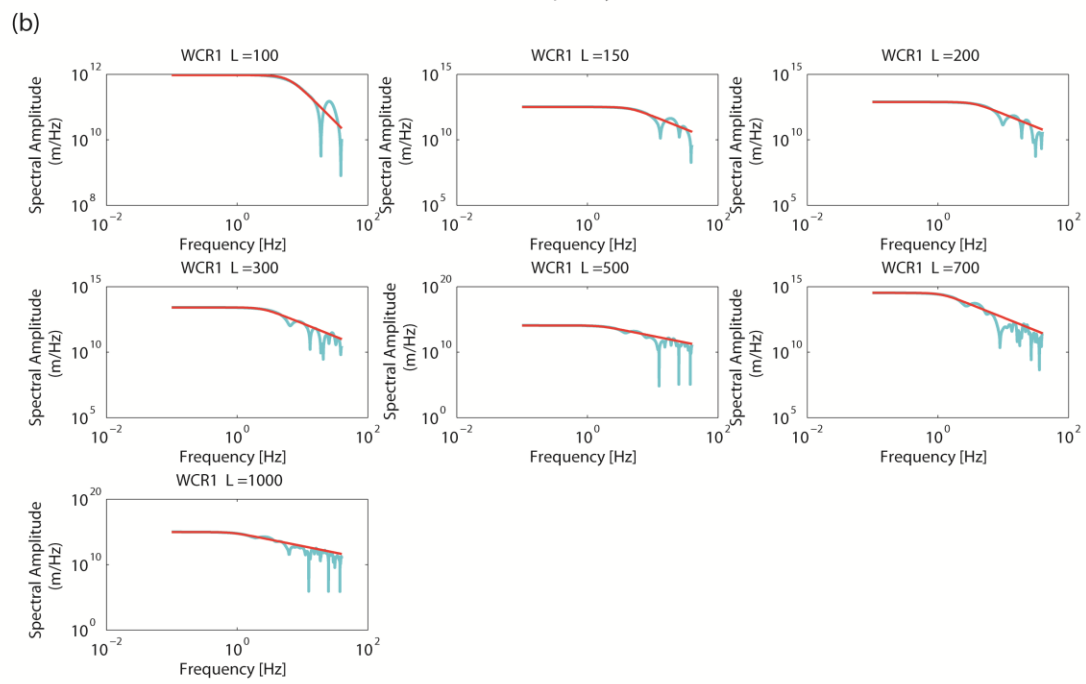
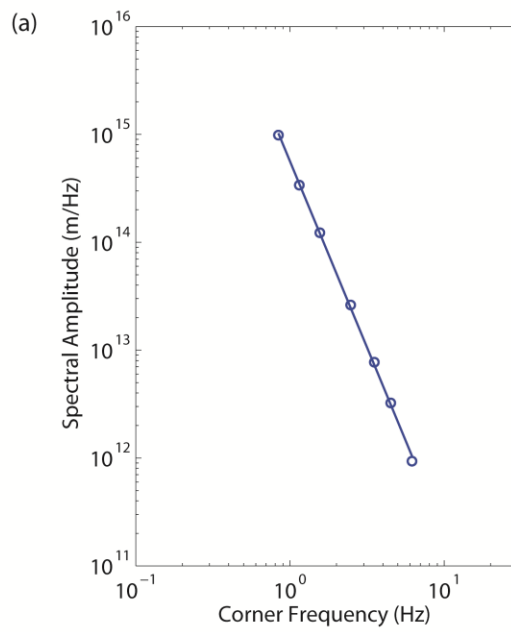


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914 Figure 10

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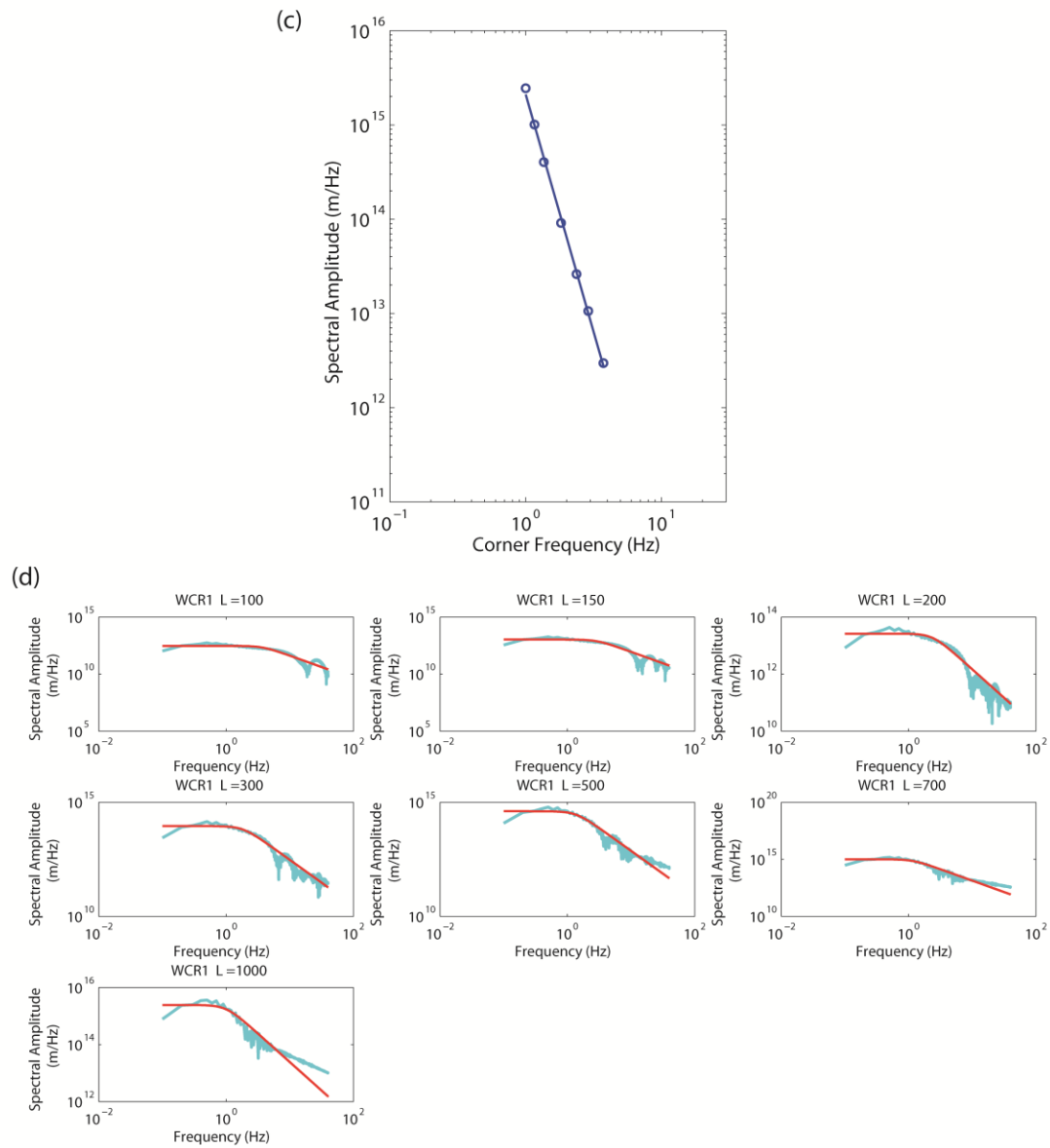
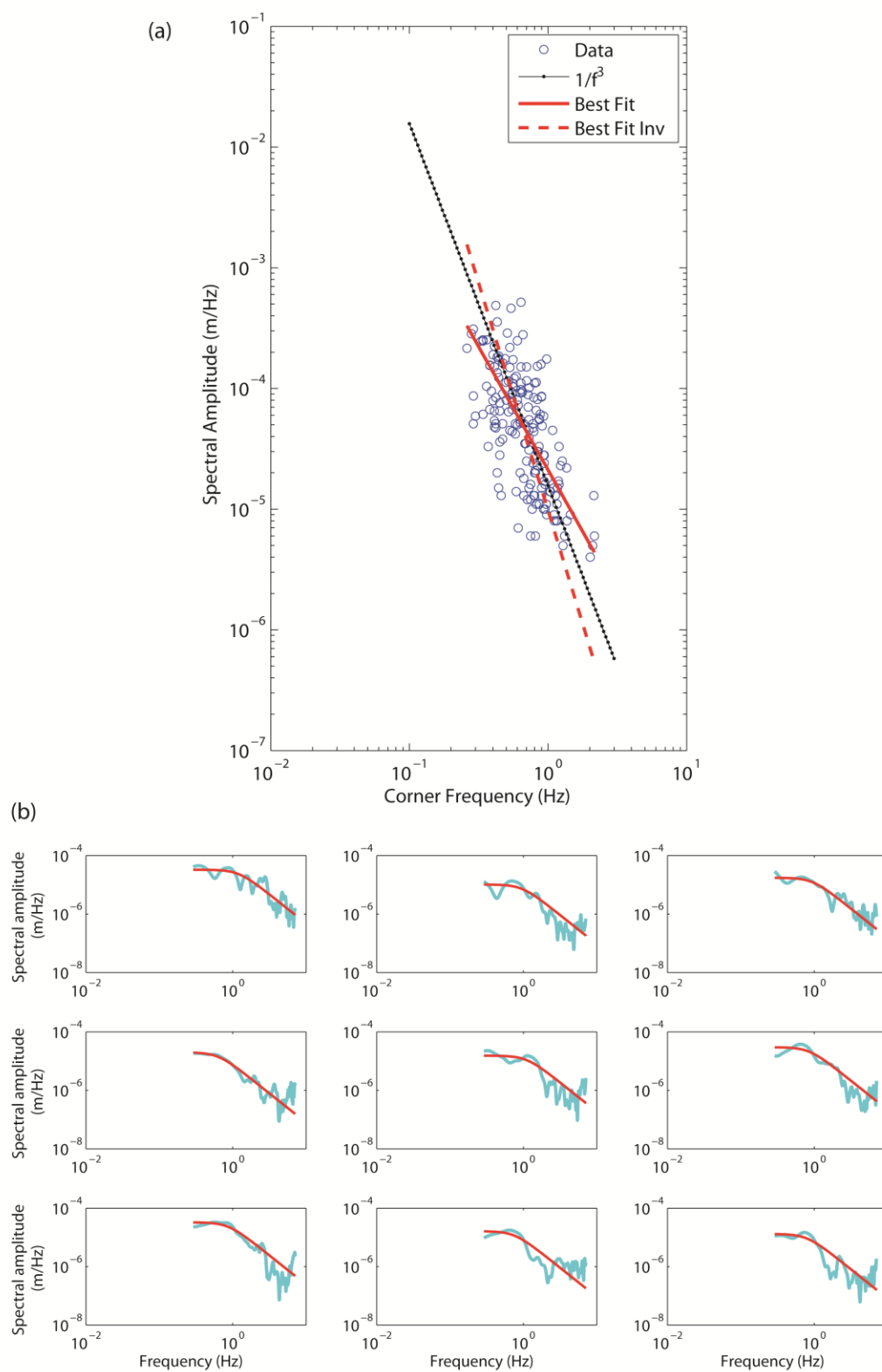


Figure 11



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924 Figure 12